# Towards Design Recovery from Observations

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**Abstract.** This paper proposes an algorithm for the construction of an MSC graph from a given set of actual behaviors of an existing concurrent system which has repetitive subfunctions. Such a graph can then be checked for safe realizability and be used as input to existing synthesis techniques.

## 1 Introduction

A concurrent system consists of two or more processes communicating among themselves via message exchanges. Each individual functionality (i.e., intended or actual behavior) of such a system can be viewed as a sequence of subfunctions. Often, depictions of individual intended behaviors of a concurrent system are given by designers as Message Sequence Charts (MSCs) [1, 2]. An individual MSC is a visual description of a series of message exchanges among communicating processes in a concurrent system where the local view of the message exchanges is a total order with respect to each process but the global view is a partial order. A tuple consisting of a local view for each process of the message exchanges depicted in an MSC uniquely determines that MSC. Thus, an MSC represents a partial order execution of a concurrent system which stands for a set of linearizations (total order executions of the system) determined by considering all possible interleavings of concurrent message exchanges implied by the partial order.

Formal semantics associated with MSCs provides a basis for their analysis such as detecting timing conflicts and race conditions [3], non-local choices [4], model checking [5], and checking safe realizability [6] (revised version appeared as [7]). Safe realizability is a property that characterizes whether behaviors represented by a given set of MSCs can be realizable by some deadlock-free implementation of communicating processes. [7] shows that if the given set of MSCs is safely realizable then an approach similar to existing synthesis algorithms can be used to synthesize a deadlock-free design. If it is not, then unspecified (and possibly unwanted) MSCs that are implied can be detected and fed back to the design process. While checking for safe realizability of a given set of MSCs that does not imply any repetitive system subfunctions can be done in polynomial time [7], that of a given bounded MSC graph is in EXPSPACE [8], which is later shown to be EXPSPACE–complete [9].

Design representations are helpful not only for implementing software systems, but also for software maintenance, e.g. to detect and eliminate errors in a system, to extend the capability of a system, or to adapt a system to different operating environments. Further, the developers of a new software system whose functionality contains some of the functionality of an existing system can benefit by using the related part of the design of the existing system. However, up-to-date or complete designs of many existing systems may not always be available.

One of the aims of the reverse engineering [10, 11] is to recover the design of an existing system from the run time behavior of its implementation. In this paper, we consider the reverse engineering of designs of existing concurrent systems from given sets of observations of their implementations. Here, a given set of observations consists of individual linearizations of a set of MSCs that is not given. We propose an algorithm for constructing an MSC graph from a given set of observations of an existing concurrent system as a representation of the system's design.

We assume that every repetitive subfunction of the system (if any) is represented in the given set of observations at least twice: once with no occurrence or one occurrence, and once with two or more consecutive occurrences. This assumption stems from the fact that some repetitive subfunctions can be skipped during executions, whereas others cannot.

When the resulting graph is acyclic, it is guaranteed that the system's functionality is free from repetitive subfunctions. Otherwise, the resulting MSC graph is cyclic due to the existence of repetitive subfunctions in system's behavior. In either case, the resulting MSC graph may then be checked for safe realizability and, when found safely realizable, can be used directly as input to the existing automated synthesis techniques.

The rest of the paper is organized as follows: Section 2 introduces the terminology and notation used throughout the paper. Section 3 gives the formal definition of the problem. Section 4 presents the construction of an MSC graph from a given set of observations. Section 5 discusses some open problems and gives the concluding remarks.

### 2 Preliminaries

The notation we will be using is directly adopted from [7]. A concurrent system  $\mathcal{P}$  is a set of processes  $\mathcal{P} = \{P_1, P_2, \ldots, P_n\}$ , communicating with each other by passing messages from an alphabet  $\Sigma$ , over infinite slot (not necessarily FIFO) buffers. An event labeled as snd(i, j, a) denotes the transmission of a message  $a \in \Sigma$  by the process  $P_i$  to the process  $P_j$ . Similarly, an event labeled as rcv(j, i, a) denotes the reception of a message a by the process  $P_j$ , which must have been sent by  $P_i$ .

We use [n] to denote the set  $\{1, 2, ..., n\}$ . Let  $\hat{\Sigma}_i^s = \{snd(i, j, a) | j \in [n], a \in \Sigma\}$ ,  $\hat{\Sigma}_i^r = \{rcv(i, j, a) | j \in [n], a \in \Sigma\}$ , and  $\hat{\Sigma}_i = \hat{\Sigma}_i^s \cup \hat{\Sigma}_i^r$  be the set of send event labels, the set of receive event labels, and the set of event labels of the process  $P_i$ , respectively. Then we define,  $\hat{\Sigma}^s = \bigcup_{i \in [n]} \hat{\Sigma}_i^s$ ,  $\hat{\Sigma}^r = \bigcup_{i \in [n]} \hat{\Sigma}_i^r$ , and  $\hat{\Sigma} = \hat{\Sigma}^s \cup \hat{\Sigma}^r$ , as the set of send event labels, set of receive event labels, and the set of receive event labels, and the set of receive event labels, and the set of event labels, respectively.

A word w over an alphabet  $\hat{\Sigma}$  is a finite sequence of elements from that alphabet. For two words w and w', juxtaposition of the two words, ww', denotes the concatenation of w and w'. w' is said to be a *prefix* of w, if there exists w'' such that w = w'w''. For an integer  $k \geq 0$ ,  $w^{(k)}$  denotes the concatenation of k copies of w, where  $w^{(0)}$  is defined to be the empty word. We will use the notation  $w^*$  to denote concatenation of 0 or more copies, and  $w^+$  to denote concatenation of 1 or more copies of the word w.

Given a word w over  $\hat{\Sigma}$  and an event label  $\alpha \in \hat{\Sigma}$ , let  $\#(w, \alpha)$  be the number of occurrences of  $\alpha$  in w. w is said to be *well-formed* if  $\forall \text{prefix } w'$  of w,  $\forall i, j \in [n]$ and  $\forall a \in \Sigma, \#(w', snd(i, j, a)) - \#(w', rcv(j, i, a)) \geq 0$ . In other words, every receive event must be preceded by a matching send event. w is said to be *complete* if  $\forall i, j \in [n]$  and  $\forall a \in \Sigma, \#(w, snd(i, j, a)) = \#(w, rcv(j, i, a))$ . That is, every message a sent by  $P_i$  to  $P_j$  must be received by  $P_j$ , within the word.

Given a word w and a set K, we use  $w|_K$  (projection onto K) to denote the word that is derived by removing all the elements in w that are not in K. We use the same notation to denote the restriction of the domain of a binary relation R onto a set K. That is,  $R|_K$  is the projection of R onto K.

Again, we directly adopt the formal definition of an MSC as introduced in [7]. A  $\Sigma$ -labeled MSC M for a concurrent system  $\mathcal{P}$  is composed of the following components<sup>1</sup>:

- (i) A finite set S of send events and a finite set R of receive events. Let  $E = S \cup R$ .
- (ii) A mapping  $l: E \to \hat{\Sigma}$  that maps each event to a label such that  $l(S) \subseteq \hat{\Sigma}^S$ and  $l(R) \subseteq \hat{\Sigma}^R$ .
- (iii) A bijection  $f: S \to R$  mapping each send event e with its matching receive event such that if l(e) = snd(i, j, a) then l(f(e)) = rcv(j, i, a).
- (iv) A mapping  $p: E \to [n]$  such that if l(e) = snd(i, j, a) then p(e) = i, and if l(e) = rcv(i, j, a) then p(e) = i. p simply gives the process on which e occurs. Let  $E_i = \{e \in E | p(e) = i\}$  be set of events of  $P_i$  for  $i \in [n]$ .
- (v) For each  $i \in [n]$ , a total order  $\leq_i$  on  $E_i$ , such that when the relation  $\leq$  is defined to be

$$\leq \triangleq \bigcup_{i \in [n]} \leq_i \bigcup \{ (s, f(s)) | s \in S \}$$

the transitive closure  $\leq^*$  of  $\leq$  is a partial order on E.

The total order  $\leq_i$  on  $E_i$  gives a strict execution order of the events of  $P_i$  as seen on the vertical process lines of  $P_i$  in the visual representation of the MSC.

<sup>&</sup>lt;sup>1</sup> Note that, this definition of MSCs does not include the notion of *co-region* (the region on a process line in which the events of the processes are not ordered) in MSCs which is also omitted in this paper.

The pairs  $(s, f(s)) \in \leq$  correspond, in the visual representation, to the message passing arrows from the process line of p(s) to the process line of p(f(s)).

Throughout the paper,  $\Sigma$  and  $\mathcal{P}$  are assumed to be fixed and all the MSCs mentioned will be  $\Sigma$ -labeled and defined on  $\mathcal{P}$ . Let  $\mathbb{M}$  denote the set of all  $\Sigma$ -labeled MSCs for  $\mathcal{P}$ .

Let |E| denote the cardinality of the set E. A permutation of the events E of an MSC as  $e_1e_2...e_{|E|}$  is valid when  $\forall i, j \in [|E|], e_i \leq *e_j$  implies  $i \leq j$ . In other words, the total order induced by the given permutation on E is consistent with the partial order  $\leq^*$ . A word w on  $\hat{\Sigma}$  is a linearization of an MSC M if there exists a valid permutation  $e_1e_2...e_{|E|}$  of M such that  $w = l(e_1)l(e_2)...l(e_{|E|})$ . The language of an MSC M, denoted by L(M), is the set of all linearizations of M. Two MSCs M and M' are considered to be equal, M = M', iff L(M) = L(M').

Note that, by definition, if  $w \in L(M)$ , then w is well-formed and complete. Further note that,  $\forall w, w' \in L(M), w|_{\Sigma_i} = w'|_{\Sigma_i}$ . In other words, the projections of the words in L(M) onto the event labels of a process is unique. This follows from the fact that all the valid permutations of M must respect the total order  $\leq_i$  which is included in  $\leq^*$ . In fact, this unique word, which will be denoted by  $M|_i$ , is the concatenation of the labels of the events that appear on the vertical line of  $P_i$  in the visual representation of M. Therefore, as shown in [7], given a well-formed and complete word w, there exists a unique MSC M, such that  $w \in L(M)$ , under a non-degeneracy assumption (that there is no message overtaking between same labeled events) which we also adopt in this paper. We will denote this unique MSC by msc(w). We also let  $\overline{w} = L(msc(w))$ .

Due to this fact, an MSC can be characterized by the sequence of sequences of the event labels that appear on the processes, i.e.  $M = \langle M|_i \mid i \in [n] \rangle$ . Given such a sequence, the actual MSC can be constructed easily as explained in [7]. Roughly, the procedure is to scan each  $M|_i$  starting from the beginning. During this scanning, a send event with a label snd(i, j, a) is matched with the first not-yet-matched receive event with a label rcv(j, i, a) in  $M|_j$ .

**Proposition 1.** Let M and M' be two MSCs. M = M' iff for each process  $P_i$ ,  $M|_i = M'|_i$ .

*Proof.* The proof follows from the fact that MSCs are fully characterized by their projections onto the event labels in the processes as explained above.  $\Box$ 

Consider the visual representation of an MSC M and imagine that we draw a line through M by crossing each process line exactly once, and without crossing any message arrows. Such a line divides M into two parts  $M_p$  (the part above the cutting line) and  $M_s$  (the part below the cutting line).  $M_p$  and  $M_s$  can be shown to be MSCs again. In fact,  $M_p$  and  $M_s$  are, what we are going to call below, a prefix of M and a suffix of M, respectively.

Formally, given two MSCs M and M', with the set of events respectively E and E', M' is said to be a *prefix* (resp. *suffix*) of M, iff:

- (i)  $E' \subseteq E$ .
- (ii)  $e \in E'$  implies  $\forall e' \in E$ , if  $e' \leq * e$  then  $e' \in E'$  (resp.  $e \in E'$  implies  $\forall e' \in E$ , if  $e \leq * e'$  then  $e' \in E'$ )
- (iii)  $e \in E' \cap S$  implies  $f(e) \in E'$  (resp.  $e \in E' \cap R$  implies  $f^{-1}(e) \in E'$ , where  $f^{-1}$  is the inverse of the bijection f)
- (iv)  $S' = S \cap E', R' = R \cap E', l' = l|_{E'}, f' = f|_{E'}, p' = p|_{E'}, and \forall i \in [n], \leq_i' = \leq_i |_{E'}.$

The imaginary cutting line mentioned in the intuitive explanation above is the one that crosses  $P_i$ 's line right below (resp. right above) the largest (resp. the smallest) event  $e \in E'_i$  with respect to the total order  $\leq_i$ .

Let M,  $M_p$  and  $M_s$  be MSCs with the corresponding set of events E,  $E_p$ and  $E_s$  such that  $M_p$  is a prefix of M,  $M_s$  is a suffix of M,  $E_p \cap E_s = \emptyset$  and  $E = E_p \cup E_s$ . Then, M is said to be the *sequential composition* of  $M_p$  and  $M_s$ , denoted by the juxtaposition of  $M_p$  and  $M_s$  as  $M_pM_s$ . Given two MSCs M' and M'',  $L(M'M'') = \{w | w \in \overline{w'w''}, w' \in L(M'), w'' \in L(M'')\}.$ 

For an integer  $k \ge 0$ ,  $M^{(k)}$  denotes the sequential composition of k copies of M, where  $M^{(0)}$  is defined to be the empty MSC, i.e. an MSC with the empty set of events. We will use the notation  $M^*$  to denote sequential composition of 0 or more copies, and  $M^+$  to denote sequential composition of 1 or more copies of the MSC M.

While describing the scenarios that a concurrent system must perform, a set of MSCs can be used. However, when this set gets large, it is usually presented in a more structured way by using High Level MSCs, or HMSCs, which is formally equivalent to an MSC graph given below. An MSC graph is a labeled transition system  $G = (V, v_0, v_f, T)$ , where V is a finite set of nodes,  $v_0, v_f \in V$  are the entry and exit nodes (respectively). The relation  $T \subseteq V \times \mathbb{M} \times V$  gives the edges between the nodes with the labels from  $\mathbb{M}$ . A *path* in G is a sequence of edges

$$(v_1, M_1, v_2)(v_2, M_2, v_3)(v_3, M_3, v_4) \cdots (v_m, M_m, v_{m+1})$$

Such a path is said to start at node  $v_1$  and end at node  $v_{m+1}$ . The language of a path is given by the concatenation of the language of the MSCs that appear on the edges,  $L(M_1)L(M_2)\cdots L(M_m)$ . Given an ordered pair of nodes (v, v'), the language of the pair (v, v'), denoted by L(v, v'), is the union of the languages of all the paths that start at v and end at v'. The language of a node v, denoted by L(v), is  $L(v, v_f)$ . The language of an MSC graph G is defined as  $L(G) = L(v_0)$ . We will use the notation  $v \xrightarrow{M} v'$  to denote  $(v, M, v') \in T$ .

### 3 Problem Definition

Each function implemented by a concurrent system can be viewed as a combination of some subfunctions. For example, in a file transfer function of a communication protocol, we may have connection establishment (CE), data transfer



Fig. 1. An example MSC Graph

(DT), connection release (CR) subfunctions. If one could identify the subfunctions as they are being executed, then a typical execution would consist of the following steps:

$$CE, DT, DT, ..., DT, CR$$
(1)

Based on the size of the data being transferred, the subfunction DT would be executed repeatedly, as many times it is required to transfer the amount of data at hand. If we consider how one would start describing such a function at an abstract level when the system was first built, it is not unreasonable to imagine that an MSC graph similar to the one given Figure 1 had been used.

In the context of reverse engineering, several attempts appeared in the literature to recover the design of an implementation from a given set of observations [12, 13, 14, 15, 16, 17]. However, if the sequence given in (1) is reverse engineered with the current techniques, the existence of repetitions of DT will cause problems. In general, it is not possible to decide if the repetitions of DT in (1) are due to a loop or due to the sequential appearance of DT in the design. Current techniques favor the latter and therefore, do not attempt to recover a design with the loops. In this paper, we will introduce a method that will help recover designs with loops.

As observations, we consider the execution logs (logs of message transmissions and receptions of the processes) of an implementation Imp of a concurrent system. In other words, if  $\Sigma$  is the set of messages used for the communication between the processes of Imp, then an observation is a well-formed and complete word over  $\hat{\Sigma}$ . We assume that an observation  $w \in \hat{\Sigma}^*$  corresponds to a complete execution of a single function of Imp, and the functions are assumed to start from the initial system state, and end back at the initial system state, without going through the initial system state. That is, if w is an observation and the system is at the initial state, then after performing the message exchanges given in w (in the order they appear in w), the system goes back to the initial state right after the last member of w (which must be a reception since w is complete) is realized. Furthermore, at no point in w, the system must be in the initial system state, since otherwise the prefix of w up to that point would be considered as a separate observation.

Suppose that we are given a set of observations O. In Section 2, it is shown that a well-formed and complete word corresponds to a unique MSC. Consider the MSC msc(w) corresponding to an observation  $w \in O$ , and a word  $w' \in L(msc(w))$  but  $w' \notin O$ . Since the individual processes are behaving, from their local point of view, exactly in the same way for both w and w', although not given as an observation, w' must also be an observation of Imp. Only the interleaving preferences between the processes change from w to w'. Therefore, the given set of observations O, together with these implied observations, actually corresponds to a wider set which is:

$$\overline{O} = \bigcup_{w \in O} \overline{w} = \bigcup_{w \in O} L(msc(w))$$

Since each given observation in  $w \in O$  actually corresponds to an MSC msc(w), we consider our input to be the set of MSCs  $\mathcal{M} = \{msc(w) \mid w \in O\}$ , and we will consider an observation to be an MSC from now on unless stated otherwise.

In our view of a function being composed of subfunctions, we also consider a subfunction to be specified by an MSC. This can be justified by considering that all the messages sent within a subfunction will be consumed within the same subfunction. In an observation M, which is given as a single MSC, the MSCs corresponding to the subfunctions are not apparent. However, our purpose is not to identify the MSCs of all the subfunctions one by one, but rather to identify those MSCs that correspond to repetitive subfunctions.

Note that, if there are any loops in the design of Imp, and if an observation  $M \in \mathcal{M}$  is generated by more than one iteration of some loop, then there must be some repeated pattern in M where the pattern being repeated is generated by the iterations of the loop. However, the converse is not correct in general, i.e., a repeated pattern seen in an observation is not necessarily due to a loop.

To be able to infer a loop in the design by looking at observations, we demand some evidence. We do not readily accept that a repeated pattern seen in a single observation is due to a loop. However, if the same pattern is seen different number of repetitions *within the same context*, then we assume this is a sufficient evidence for the existence a loop. Below is the formal definition of the notion of this evidence.

**Definition 1.** An MSC M is said to be the basic repetitive MSC of MSC M' if  $M' = M^{(k)}$  for some  $k \ge 2$  and there does not exist a basic repetitive MSC of M.

**Definition 2.** Two MSCs  $M_1$  and  $M_2$  are said to infer M to be repetitive within the context  $M_p-M_s$  if all the following are satisfied:

- (i) M does not have a basic repetitive MSC;
- (ii)  $M_1 = M_p M^{(k)} M_s$  for some  $k \ge 2$ ;
- (iii) M is not a suffix of  $M_p$ ;
- (iv) M is not a prefix of  $M_s$ ;
- (v) either  $M_2 = M_p M_s$  (in which case M is said to be while-repetitive) or  $M_2 = M_p M M_s$  (in which case M is said to be repeat-repetitive).

Note that Definition 2 captures the essence of two different repetitive subfunctions, one which can be skipped, whereas the other cannot be skipped during the execution of the system. In order to differentiate these two different types, we call them as *while* and *repeat* repetitive respectively, by using an analogy to standard programming loop types.

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What we require in observations to infer a loop is that, there must be an observation in which the loop is iterated  $k \geq 2$  times, and there must also be another observation in which the same loop iterated the least possible number of times (which is 0 for a while loop, and 1 for a repeat loop). Furthermore, these two observations must have exactly the same prefix before the iterations of M, and exactly the same suffix after the iterations of M, that is they must appear within the same context. Under such an evidence, M will be assumed to be generated by a loop in the design, or more precisely, by the matching loops (sending and receiving matching messages) in the processes.

Suppose that M is found to be while–repetitive under the evidence of two observations  $M_1$  and  $M_2$  with the prefix  $M_p$  and suffix  $M_s$ , and suppose that Mis indeed generated by a loop in the design. Then the state right before the execution of M, and right after the execution of M are the same. Hence, any MSC in the form  $M_p M^* M_s$  must be realizable by Imp. A similar argument can be applied to show that when M is found to be repeat-repetitive, any MSC in the form  $M_p M^+ M_s$  must be realizable by Imp.

Since we assume that Imp does not go through the initial system state during the execution of an observation,  $M_p$  and  $M_s$  in Definition 2 must not be empty. This can be justified by the following observation. If M is repetitive, then the state just before and just after an iteration of M are the same. If  $M_p$  is empty, then M starts its execution from the initial state, since the observations start from the initial state. After the first iteration of M, the system will again be at the initial state. However, this is the definition of a function in our setting, hence M and  $M_s$  must be given as separate observations. Similarly, if  $M_s$  is empty, then the state after an iteration, hence before an iteration of M is the initial state, since observations are assumed to end at this state. In this case,  $M_p$ and M must be given as separate observations.

It is also important to note that, an iteration of a loop in an observation is allowed only to provide the required evidence to infer a loop. Further, each repetitive subfunction is inferred only once using the given observations. Moreover, in order to establish the relative ordering of two or more loops  $l_1, l_2, \ldots, l_n$  in an MSC graph,  $k \ge 2$  iterations of at least two loops  $l_i$  and  $l_j$  need to be given in the same observation such that the relative ordering of a pair of loops  $l_i$  and  $l_k$ can be determined from the relative ordering of two pairs of loops  $l_i$  and  $l_j$ , and  $l_i$  and  $l_k$ ,  $1 \le i, j, k \le n$ , and by transitivity.

### 4 Problem Solution

When a pair of MSCs  $M_1$  and  $M_2$  is identified within the given set  $\mathcal{M}$ , such that  $M_1$  and  $M_2$  infers M to be repetitive within the context  $M_p-M_s$ , then  $M_1$  and  $M_2$  will be represented in the output MSC graph by using either one of the following templates, depending on whether it is while-repetitive (left) or repeat-repetitive (right).

$$v_0 \xrightarrow{M_p} v \xrightarrow{M_p} v_f \qquad v_0 \xrightarrow{M_p} v \xrightarrow{M} v' \xrightarrow{M_s} v_f$$

An algorithm that will find such pairs of MSCs, must identify the context part, i.e. common prefix  $M_p$  and the common suffix  $M_s$ , and must also check if the part remaining in the middle has a basic repetitive MSC. Before presenting such an algorithm, we need to introduce the following notions on MSCs. A *common prefix* of two MSCs  $M_1$  and  $M_2$ , is an MSC M, such that M is a prefix of both  $M_1$  and  $M_2$ . The maximal common prefix of  $M_1$  and  $M_2$  is a common prefix M of  $M_1$  and  $M_2$  with the largest number of events. Similarly, M is said to be a common suffix of  $M_1$  and  $M_2$  with largest number of elements is called the maximal common suffix of  $M_1$  and  $M_2$ .

Suppose that  $M = M_p M_s$ . Given M and  $M_p$ , it is trivial to find  $M_s$ , by simply removing all the events in  $M_p$  from the first part of M. Similarly, when we are given M and  $M_s$ , removing all the events in  $M_s$  starting from the last part of M will give  $M_p$ . In both of these algorithms, we need to match the labels of the events. Let us assume that these algorithms are called as "remove\_prefix" and "remove\_suffix", respectively.

We can now present an algorithm that can check if two given MSCs identify a repetitive MSC. Without loss of generality, we assume that  $M_1$  has more events than  $M_2$ .

Recall that, in order to infer M to be repetitive from  $M_1$  and  $M_2$ , we must have  $M_1 = M_p M^{(k)} M_s$  and either  $M_2 = M_p M_s$  or  $M_2 = M_p M M_s$ . The maximal common prefix of  $M_1$  and  $M_2$  will be consisting of  $M_p$ , followed by an optional single occurrence of M. In either case, however,  $M''_2$  in Algorithm 1 given in Figure 2 must be empty (line 7). At line 10 and 11, we check if  $M''_1$  has a basic repetitive MSC, by using the algorithm "basic\_repetitive\_MSC", which is explained in Section 4.1. For the time being, assume that it returns the basic repetitive MSC of its input MSC, if there exists one, or returns the empty MSC otherwise. If such an M does not exist, we may still infer a repetitive MSC. This corresponds to the case where  $M_1 = M_p M^{(2)} M_s$  and  $M_2 = M_p M M_s$ . In this specific case, the maximal common prefix  $M_{mp}$  would be  $M_p M$ . Line 12 checks this singularity, and the correct left context is calculated at line 13.

However, if  $M_1''$  has a basic repetitive MSC M, then we decide if it is while– repetitive or repeat–repetitive, between the lines 18–23. Note that when M is found to be repeat–repetitive (line 19-20), M will be a common suffix of the maximal common prefix of  $M_1$  and  $M_2$ . In order to find the correct left context, line 19 extracts this common suffix from  $M_{mp}$ .

Note that, there may be multiple ways for dividing  $M_1$  and  $M_2$  to identify  $M_p$ , M and  $M_s$ . For example, let  $M_1 = M_a M_b M_c M_b M_c M_b M_d$  and let  $M_2 = M_a M_b M_d$ . In this case, it is possible to infer  $M_b M_c$  as while–repetitive within the context  $M_a - M_b M_d$ . However, it is also possible to infer  $M_c M_b$  as

1:  $M_{mp} = \text{maximal\_common\_prefix}(M_1, M_2);$ 2:  $M'_1$  = remove\_prefix $(M_{mp}, M_1)$ ; 3:  $M'_2$  = remove\_prefix $(M_{mp}, M_2)$ ; 4:  $M_s = \text{maximal\_common\_suffix}(M'_1, M'_2);$ 5:  $M_1'' = \text{remove\_suffix}(M_s, M_1');$ 6:  $M_2'' = \text{remove\_suffix}(M_s, M_2');$ 7: if  $M_2''$  is not empty or  $M_{mp}$  is empty or  $M_s$  is empty then  $M_1$  and  $M_2$  do not infer a repetitive MSC 8: 9: else 10: $M = \text{basic\_repetitive\_MSC}(M_1'');$ if M is empty then 11:if  $M_1''$  is a suffix of  $M_{mp}$  then 12: $M_p = \text{remove\_suffix}(M_{mp}, M_1'');$ 13: $M_1$  and  $M_2$  infer  $M_1''$  to be repeat-repetitive within the context  $M_p-M_s$ 14: 15:else 16: $M_1$  and  $M_2$  do not infer a repetitive MSC 17:end if else if M is a suffix of  $M_{mp}$  then 18:19: $M_p = \text{remove\_suffix}(M_{mp}, M);$ 20: $M_1$  and  $M_2$  infer M to be repeat–repetitive within the context  $M_p$ – $M_s$ 21:else 22: $M_1$  and  $M_2$  infer M to be while-repetitive within the context  $M_{mp}-M_s$ 23:end if 24: end if

**Fig. 2.** Algorithm 1 – Checking if  $M_1$  and  $M_2$  infers an MSC M to be repetitive

while–repetitive within the context  $M_a M_b - M_d$ . By convention, we prefer to keep preamble of the loop as long as possible, hence use the latter alternative. Note that, this is only a convention as both  $M_a M_b (M_c M_b)^* M_d$  and  $M_a (M_b M_c)^* M_b M_d$ have the same language. Algorithm 1 implements this convention by extracting the maximal common prefix of  $M_1$  and  $M_2$  at line 1.

We explain four elementary functions and the algorithm basic\_repetitive\_MSC referenced in Algorithm 1 in the following subsections.

#### 4.1 Finding the Basic Repetitive MSC

In this subsection, we explain how to check the existence of and find the basic repetitive MSC M of a given MSC M'.

Recall that  $M|_i$  denotes the sequence of event labels of process  $P_i$  in the MSC M. If  $M' = M^{(k)}$ , it is obvious that for each process  $P_i$ , we have

$$M'|_i = \underbrace{M|_i M|_i \cdots M|_i}_{k \text{ times}}$$

In other words, we must see these repeating patterns in the events of the processes as well. Checking if a word w' consists of repetitions of another word w

is a well-known and well-studied problem (e.g. see [18]) in pattern matching and text processing. If  $w' = w^{(r)}$ , then r is called the power of w in w' (we are only interested in integer powers, although the general theory of repetitions in words considers rational powers as well), and w is called a root of w'. If w cannot be written as a repetition of another word, then it is called as primitive. Linear time algorithms exist to find the primitive root of a word. Note that a word is always a root of itself with power 1.

**Proposition 2.** Given an MSC M', let  $r_i$  be the power of the primitive root of  $M'|_i$ , where  $i \in [n]$ , and let  $r = \text{gcd}(r_1, r_2, \ldots, r_n)$ . M' has a basic repetitive MSC iff  $r \geq 2$ .

*Proof.* Assume that M' has a basic repetitive MSC, i.e.  $M' = M^{(k)}$  for some M and  $k \ge 2$ . Since the projections onto the processes must be the same,  $M'|_i = M|_i^{(k)}$ . Therefore,  $r_i = kr'_i$  where  $r'_i$  is the power of the primitive root of  $M|_i$  (note that  $M|_i$  is not necessarily primitive). Therefore k is a common divisor of  $r_1, r_2, \ldots, r_n$ , and hence  $r = gcd(r_1, r_2, \ldots, r_n) \ge k \ge 2$ .

For the proof of the reverse direction, assume that  $r \geq 2$ . Consider an MSC M, where  $M|_i$  is the first  $|E'_i|/r$  event labels in  $M'|_i$ . Note that  $M' = M^{(r)}$ , since process wise projections are the same. It remains to show that M does not have a basic repetitive MSC. In fact this must be true, since if  $M = M''^{(r')}$  for some  $r' \geq 2$ , then we must have  $M' = M''^{(rr')}$ . However in this case, rr', which is strictly greater than r would be a common divisor of  $r_1, r_2, \ldots, r_n$ , contradicting with the fact that  $r = gcd(r_1, r_2, \ldots, r_n)$ .

### 4.2 Functions on Maximal Common Prefix–Suffix, and Prefix–Suffix Removal

Finding the maximal common prefix of two words is trivial, and based on scanning and comparing the elements of the words starting from the beginning and stopping when a difference is seen.

Finding the maximal common prefix of two MSCs is not as trivial as the case of words, since we require the prefix to be an MSC as well. Let M' and M'' be two MSCs. Consider again the sequence of event labels  $M'|_i$  and  $M''|_i$  of process  $P_i$  on M' and M''. Note that  $M'|_i$  and  $M''|_i$  are words. Let  $w_i$  be the maximal common prefix of the words  $M'|_i$  and  $M''|_i$ . Note that the sequence of event labels  $\langle w_i \mid i \in [n] \rangle$  does not necessarily characterize an MSC. However, this problem can be solved by removing some of the suffixes of  $w_i$ 's. Recall the procedure explained shortly in Section 2, for building an MSC based on a sequence of sequence of event labels. This procedure can be adapted to eliminate the problematic suffixes in  $w_i$ 's while finding the maximal common prefix in the following way. Initially, all the event labels in  $w_i$ 's are unmarked. Then perform a scan on each  $w_i$  starting from the beginning. For each send event label of the form snd(i, j, a) in  $w_i$ , find the first unmarked event label of the form snd(i, j, a) in  $w_i$  instances under consideration, and proceed to

the next send event in  $w_i$ . When we mark two such events, they are called as marking pairs. It is necessary to remember this association since, if and when one of them is removed, the other will also be removed in the second phase of this procedure. If no such an unmarked event could be found in  $w_j$ , then leave snd(i, j, a) and all the remaining events in  $w_i$  as unmarked. After this marking phase, we have an iterative suffix removal phase. For each  $w_i$ , the suffix of  $w_i$ that starts with the first unmarked event label is removed. Note that, some of the event labels in such a suffix may be marked. While removing such a marked event label, the mark of its marking pair (which must also be present in some  $w_j$ as marked) is removed. This iteration continues until all the event labels in all the  $w_i$ 's are marked. The remaining event labels characterize an MSC which is the maximal common prefix. Finding the maximal common suffix of two MSCs can be performed in a similar way, by adapting the approach in the procedure explained above.

Given an MSC M and a prefix M' of M, removing the prefix M' can be performed by removing the event label sequence  $M'|_i$  from the first part of  $M|_i$  for each process  $P_i$ . Similarly, the removal of a suffix M' of M would be performed by removing the event label sequence  $M'|_i$  from the last part of  $M|_i$ for each process  $P_i$ .

#### 4.3 Forming the Final MSC Graph

Algorithm 2 given in Figure 4 is used to produce an MSC graph based on a given set of MSCs  $\mathcal{M}$ . It has two phases. The first phase considers every pair of MSCs  $M_1$  and  $M_2$  in  $\mathcal{M}$  and checks whether  $M_1$  and  $M_2$  infer a repetitive MSC. The output of the first phase is an MSC graph with a special structure. For each pair of MSCs that infer a repetitive MSC, a separate subgraph, that is disjoint with the rest of the graph except at  $v_0$  and  $v_f$ , is created. Such a subgraph has a different structure depending on whether the inferred MSC is while— or repeat—repetitive, which are shown in Figure 3 at the top and in the middle, respectively. If an MSC M does not infer a repetitive MSC by pairing with another MSC, then a subgraph which consists of only  $(v_0, M, v_f)$  is created, as shown at the bottom in Figure 3. We will call these subgraphs as paths below. These paths will be referenced using the labels of the edges. The loops in the labels of the paths will be represented by using  $\star$ . The second column of Figure 3 gives the label template associated with each path type.

As an example for the execution of the first phase, let us suppose that initially we have three MSCs

$$M_{a} = M_{1}M_{2}M_{2}M_{3}M_{4}M_{5},$$
  

$$M_{b} = M_{1}M_{2}M_{2}M_{3}M_{4}M_{4}M_{5},$$
  

$$M_{c} = M_{1}M_{3}M_{4}M_{5}.$$

 $M_a$  and  $M_b$  infer  $M_4$  to be repeat-repetitive within the context  $M_1 M_2^{(2)} M_3 - M_5$ . Hence

$$M_d = M_1 M_2^{(2)} M_3 M_4 M_4^* M_5$$



Fig. 3. Three different path types

is inferred as a path in G. Similarly,  $M_a$  and  $M_c$  infer  $M_2$  to be a while-repetitive within the context of  $M_1$ – $M_3M_4M_5$ . So

$$M_e = M_1 M_2^{\star} M_3 M_4 M_5$$

is inferred as a path in G.

Note that the subgraph generated from  $M_1$  and  $M_2$  is guaranteed to represent both  $M_1$  and  $M_2$ , i.e. the language of  $M_1$  and  $M_2$  are included in the language of the generated subgraph. Thus,  $M_1$  and  $M_2$  are marked for deletion since we generated a new path from them. However, if for an MSC  $M_1$ , there does not exist an MSC  $M_2$  which infers a repetitive MSC, then  $M_1$  will simply be put into G and left unmarked. At the end of the first phase, there is no other loop left to be inferred. However, all possible relative positions of these loops must be represented in the final MSC graph G' which is constructed in the second phase of Algorithm 2.

The MSC graph G constructed by the first phase can be nondeterministic. In other words, there may be two different paths with a nonempty common prefix. In general, there is no guarantee that the system state is the same after the execution of the same prefix along these different paths, since the observations only give the message exchanges, and the local actions within the processes are hidden from the observer. There needs to be some evidence in the observations that allow some paths to be merged. Especially when a given observation M is used in the generation of two different paths  $p_1$  and  $p_2$  with labels  $M_1$  and  $M_2$ respectively, the execution of  $p_1$  and  $p_2$  also corresponds to the execution of M. Hence the system state along  $p_1$  and  $p_2$  need to be merged.

The second phase of Algorithm 2 performs the merging of paths using Algorithm 3 given in Figure 5. Since we need to know the actual observations from which a path p is generated, the first phase of the algorithm associates this information to the generated path p by src(p).

In the example above, after the first phase, MSCs  $M_a$ ,  $M_b$  and  $M_c$  are marked and thus removed, and we have the paths corresponding to  $M_d$  and  $M_e$  added to G. In the second phase, there are two paths  $M_d$  and  $M_e$  in G. Since the sources of these two paths have a nonempty intersection, they will be in the same partition, which is actually the only partition of paths in this example.

```
1: /* phase 1: infer loops and form G^*/
 2: initially all the MSCs in \mathcal{M} are unmarked
 3: generate the initial and the final nodes v_0 and v_f in G
 4: for each pair M_1, M_2 \in \mathcal{M} do
      if M_1 and M_2 infers an MSC M to be repetitive within a context M_p-M_s then
 5:
 6:
         mark both M_1 and M_2
 7:
         if M is while–repetitive then
           generate a new path p in G given below, where v is a new node
 8:
           p = \{(v_0, M_p, v), (v, M, v), (v, M_s, v_f)\}
 9:
         else
           generate a new path p in G given below, where v and v' are new nodes
10:
           p = \{(v_0, M_p, v), (v, M, v'), (v', M, v'), (v', M_s, v_f)\}
11:
         end if
12:
         let src(p) = \{M_1, M_2\}
13:
       end if
14: end for
15: for each unmarked MSC M do
       generate a new path p = \{(v_0, M, v_f)\}
16:
       let src(p) = \{M\}
17:
18: end for
19: /* phase 2: merge paths and form G' */
20: let G' be an empty graph
21: obtain a partition \Pi of the set of paths such that two paths p, p' are in the same
    subset P of \Pi iff \exists a sequence of paths p_1, p_2, \ldots, p_k where p_j \in P, 1 \leq j \leq k,
    p = p_1, p' = p_k, and for 1 \le i < k, src(p_i) \cap src(p_{i+1}) \ne \emptyset
22: for all P \in \Pi do
      insert merge(P) into G'
23:
24: end for
```

Fig. 4. Algorithm 2 – Building the MSC graph based on a set of MSCs  $\mathcal{M}$ 

Hence, the for loop at lines 22–24 in Algorithm 2 will iterate only once, and will insert the merging of  $M_d$  and  $M_e$  into G'.

In Algorithm 3, we consider every path as a set of three edges :  $(v_0, M_p, v_1)$ ,  $(v_1, M, v_1)$  and  $(v_1, M_s, v_f)$ .  $M_p$ , M and  $M_s$  will be referred to as the prefix, loop and the suffix labels of the path, respectively. Note that, if the path is generated for a repeat repetitive subfunctionality, then we consider the first iteration of the loop as embedded in the prefix label.

Note that, G' produced by the second phase will effectively have the loops in G placed in their relative order, which also includes placing a loop into another, i.e. nesting of the loops. Deciding the relative orders of the loops in different paths in the merged path is based on having a common observation used in the generation of these paths. For instance, see the example given above.

Note that, Algorithm 3 depends on tracing  $M_pM_s$  on the path  $p_m$  (which is actually an MSC graph) accumulated so far. Given an MSC M and an MSC graph G, it is known that deciding if  $M \in L(G)$  is NP-complete [8, 19]. For-

```
1: let p be a path in P whose prefix label is the shortest among other paths in P
2: let p_m = p
3: let src(p_m) = src(p)
4: let P = P - \{p\}
5: while P is not empty do
      let p be a path in P such that src(p) \cap src(p_m) \neq \emptyset and the prefix label of p is
6:
      the shortest among other such paths in P.
7:
      src(p_m) = src(p_m) \cup src(p)
      P = P - \{p\}
8:
9:
      trace the concatenation of the prefix label M_p and the suffix label M_s of p in p_m
      (by skipping \varepsilon edges)
      if during this trace M_p ends in the middle of an edge in p_m then
10:
11:
         insert a new node v in the middle of that edge in p_m
12:
         insert a new edge (v, M, v) in p_m where M is the loop label of p
13:
      else
14:
         let v be the node at which the trace of M_p has ended
         if during the trace of M_p, v is visited exactly once then
15:
           insert a new edge (v, M, v) in p_m where M is the loop label of p
16:
17:
         else
18:
           let (v, M', v') be the edge which is not used during the trace of M_p
19:
           remove the edge (v, M', v')
           insert a new node v'' in p_m
20:
           insert a new edge (v'', M', v')
21:
22:
           insert a new edge (v, \varepsilon, v'')
           insert a new edge (v'', M, v'')
23:
24:
         end if
25:
      end if
26: end while
27: return (p_m)
```

Fig. 5. Algorithm 3 – Merging paths in a partition P

tunately, in principle, tracing of  $M_p M_s$  on  $p_m$  corresponds to the case given in Theorem 6 of [8] with a time complexity of  $O(|p_m| \times |M_p M_s|)$ .

### 5 Conclusion

We have presented an algorithm to derive an MSC graph G' from a given set of observations of an existing implementation of a concurrent system. This algorithm is based on inferring repetitive subfunctions from a given set of observations. The language of the MSC graph G' derived consists of all the given observations and the inferred observations, in which the loops and their relative positions are all explored. And thus, the language of the MSC graph G' is a design representation of the existing system.

An interesting problem that remains open is the following. When the evidences of some loops are missing in the given set of observations, generated subgraphs may provide these missing evidences. For example, assume that initially we have three MSCs  $M_a = M_1 M_2^{(2)} M_3 M_5$ ,  $M_b = M_1 M_2^{(2)} M_3 M_4^{(2)} M_5$ , and  $M_c = M_1 M_3 M_4^{(3)} M_5$ .  $M_a$  and  $M_b$  infers  $M_4$  to be while-repetitive within the context  $M_1 M_2^{(2)} M_3 - M_5$ . Hence  $M_d = M_1 M_2^{(2)} M_3 M_4^* M_5$  is generated. Although  $M_c$  does not infer any repetitive subfunctionality with  $M_a$  or  $M_b$ , it infers  $M_2$  to be while-repetitive within the context  $M_1 - M_3 M_4^{(3)} M_5$  when it is considered together with  $M_e = M_1 M_2^{(2)} M_3 M_4^{(3)} M_5$  which is obtained by instantiating  $\star$  by 3 in  $M_d$ . However, these new repetitive subfunctions must be confirmed by the observer. Hence the question is, can and how an MSC graph, which is a design representation of the existing system, be generated under such missing evidences.

It will also be interesting to consider the effects of a) the number of occurrences of repetitive subfunctions in the given set of observations to be a fixed value, and b) some apriori knowledge of the structure of the communicating processes on the derivation of an MSC graph.

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